CSE 167: Introduction to Computer Graphics Lecture #5: Rasterization

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Announcements

Homework project #2 due this Friday, October 12

- To be presented starting 1:30pm in lab 260
- Also present late submissions for project #1

Lecture Overview

- Culling
- Clipping
- Rasterization
- Visibility
- Barycentric Coordinates

Culling

Goal:

Discard geometry that does not need to be drawn to speed up rendering

- Types of culling:
 - View frustum culling
 - Occlusion culling
 - Small object culling
 - Backface culling
 - Degenerate culling



View Frustum Culling

Triangles outside of view frustum are off-screen

Done on canonical view volume





Images: SGI OpenGL Optimizer Programmer's Guide

Videos

Rendering Optimisations - Frustum Culling

http://www.youtube.com/watch?v=kvVHp9wMAO8&feature=r elated

View Frustum Culling Demo

http://www.youtube.com/watch?v=bJrYTBGpwic

Bounding Box

- Rectangular box, parallel to object space coordinate planes
- Box is smallest box containing the entire object



Image: SGI OpenGL Optimizer Programmer's Guide

Occlusion Culling

Geometry hidden behind occluder cannot be seen

Complex algorithm





Images: SGI OpenGL Optimizer Programmer's Guide

Video

Umbra 3 Occlusion Culling explained

http://www.youtube.com/watch?v=5h4QgDBwQhc

Small Object Culling

Object projects to less than a specified size

 Cull objects whose screen-space bounding box is less than a threshold number of pixels

Backface Culling

- Consider triangles as "one-sided", i.e., only visible from the "front"
- Closed objects
 - If the "back" of the triangle is facing the camera, it is not visible
 - Gain efficiency by not drawing it (culling)
 - Roughly 50% of triangles in a scene are back facing

Backface Culling

 Convention: Triangle is front facing if vertices are ordered counterclockwise





- OpenGL allows one- or two-sided triangles
 - One-sided triangles: glEnable(GL_CULL_FACE); glCullFace(GL_BACK)
 - Two-sided triangles (no backface culling): glDisable(GL_CULL_FACE)

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Backface Culling

Compute triangle normal after projection (homogeneous division)

$$\mathbf{n} = (\mathbf{p}_1 - \mathbf{p}_0) \times (\mathbf{p}_2 - \mathbf{p}_0)$$

- Third component of n negative: front-facing, otherwise back-facing
 - Remember: projection matrix is such that homogeneous division flips sign of third component

Degenerate Culling

Degenerate triangle has no area

- Vertices lie in a straight line
- Vertices at the exact same place
- Normal n=0



Source: Computer Methods in Applied Mechanics and Engineering, Volume 194, Issues 48–49



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View Frustum Clipping

- Partial culling for objects intersecting the faces of the view volume
 - Need to distinguish geometry on-screen from off-screen
 - Discard off-screen geometry
- Traditional clipping
 - Split triangles that lie partly inside/outside viewing volume
- Modern GPU implementations avoid clipping
 - Hardware clips to the canonical view volume



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- Scan conversion and rasterization are synonyms
- One of the main operations performed by GPU
- Draw triangles, lines, points (squares)
- Focus on triangles in this lecture



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How many pixels can a modern graphics processor draw per second?

- How many pixels can a modern graphics processor draw per second?
- NVidia GeForce GTX 690
 - > 234 billion pixels per second
 - Multiple of what the fastest CPU could do

- Many different algorithms
- Old style
 - Rasterize edges first





- Many different algorithms
- Old style
 - Rasterize edges first
 - Fill the spans (scan lines, scan conversion)





- Many different algorithms exist
- Old style
 - Rasterize edges first
 - Fill the spans (scan lines, scan conversion)
 - Requires clipping
 - Straightforward, but not used for hardware implementation today

GPU rasteriazation today based on "Homogeneous Rasterization"

http://www.ece.unm.edu/course/ece595/docs/olano.pdf

Olano, Marc and Trey Greer, "Triangle Scan Conversion Using 2D Homogeneous Coordinates", Proceedings of the 1997 SIGGRAPH/Eurographics Workshop on Graphics Hardware (Los Angeles, CA, August 2-4, 1997), ACM SIGGRAPH, New York, 1995.

 Does not require full clipping, does not perform homogeneous division at vertices

Today in class

- Simpler algorithm
- Easy to implement
- Requires clipping



Simple algorithm

compute bbox clip bbox to screen limits for all pixels [x,y] in bbox compute barycentric coordinates alpha, beta, gamma if 0<alpha,beta,gamma<1 //pixel in triangle image[x,y]=triangleColor

Bounding box clipping trivial



- So far, we compute barycentric coordinates of many useless pixels
- How can this be improved?



Hierarchy

- If block of pixels is outside triangle, no need to test individual pixels
- Can have several levels, usually two-level
- Find right granularity and size of blocks for optimal performance



2D Triangle-Rectangle Intersection

- If one of the following tests returns true, the triangle intersects the rectangle:
 - Test if any of the triangle's vertices are inside the rectangle (e.g., by comparing the x/y coordinates to the min/max x/y coordinates of the rectangle)
 - Test if one of the quad's vertices is inside the triangle (e.g., using barycentric coordinates)
 - Intersect all edges of the triangle with all edges of the rectangle

Where is the center of a pixel?

- Depends on conventions
- With our viewport transformation:
 - ▶ 800 x 600 pixels \Leftrightarrow viewport coordinates are in $[0...800] \times [0...600]$
 - Center of lower left pixel is 0.5, 0.5
 - Center of upper right pixel is 799.5, 599.5



Shared Edges

- Each pixel needs to be rasterized exactly once
- Resulting image is independent of drawing order
- Rule: If pixel center exactly touches an edge or vertex
 - Fill pixel only if triangle extends to the right or down



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• At each pixel, we need to determine which triangle is visible

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Painter's Algorithm

- Paint from back to front
- Every new pixel always paints over previous pixel in frame buffer
- Need to sort geometry according to depth
- May need to split triangles if they intersect



 Outdated algorithm, created when memory was expensive

Z-Buffering

Store z-value for each pixel

Depth test

- During rasterization, compare stored value to new value
- Update pixel only if new value is smaller

```
setpixel(int x, int y, color c, float z)
if(z<zbuffer(x,y)) then
  zbuffer(x,y) = z
  color(x,y) = c</pre>
```

- z-buffer is dedicated memory reserved for GPU (graphics memory)
- Depth test is performed by GPU

Z-Buffering

Problem: translucent geometry

- Storage of multiple depth and color values per pixel (not practical in real-time graphics)
- Or back to front rendering of translucent geometry, after rendering opaque geometry

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Source: efg's computer lab

- What if a triangle's vertex colors are different?
- Need to interpolate across triangle
 - How to calculate interpolation weights?

Implicit 2D Lines

- Given two 2D points **a**, **b**
- Define function $f_{ab}(\mathbf{p})$ such that $f_{ab}(\mathbf{p}) = 0$ if **p** lies on the line defined by **a**, **b**



Implicit 2D Lines

Point p lies on the line, if p-a is perpendicular to the normal of the line



Use dot product to determine on which side of the line p lies. If f(p)>0, p is on same side as normal, if f(p)<0 p is on opposite side. If dot product is 0, p lies on the line.

$$f_{ab}(\mathbf{p}) = (a_y - b_y, b_x - a_x) \cdot (p_x - a_x, p_y - a_y)$$

Barycentric Coordinates

- Coordinates for 2D plane defined by triangle vertices *a*, *b*, *c*
- Any point p in the plane defined by a, b, c is $p = a + \beta (b - a) + \gamma (c - a)$ $= (I - \beta - \gamma) a + \beta b + \gamma c$
- We define $\alpha = I \beta \gamma$ => $p = \alpha a + \beta b + \gamma c$



- α , β , γ are called **barycentric** coordinates
- Works in 2D and in 3D
- If we imagine masses equal to α, β, γattached to the vertices of the triangle, the center of mass (the barycenter) is then p. This is the origin of the term "barycentric" (introduced 1827 by Möbius)



• **p** is inside the triangle if $0 < \alpha$, β , $\gamma < 1$

Barycentric Coordinates

- Problem: Given point p, find its barycentric coordinates
- Use equation for implicit lines





Division by zero if triangle is degenerate

$$\begin{aligned} \alpha &= 1 - \beta - \gamma \\ 0 &< \beta < 1 \end{aligned}$$

Barycentric Interpolation

Interpolate values across triangles, e.g., colors



$$c(\mathbf{p}) = \alpha(\mathbf{p})c_{\mathbf{a}} + \beta(\mathbf{p})c_{\mathbf{b}} + \gamma(\mathbf{p})c_{\mathbf{c}}$$

Barycentric Coordinates

Demo Applets:

http://www.ccs.neu.edu/home/suhail/BaryTriangles/applet.htm