

CSE 167:  
Introduction to Computer Graphics  
Lecture #14: Environment Mapping

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# Announcements

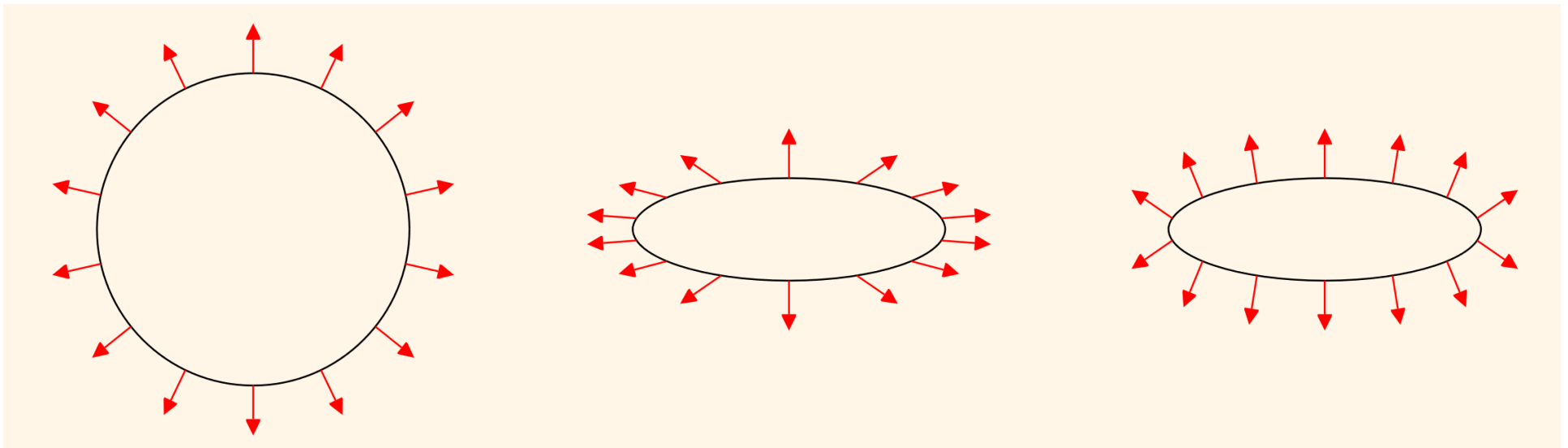
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- ▶ Tomorrow: late grading project 3
- ▶ Monday night: midterm discussion
- ▶ Tuesday: midterm exam #2
- ▶ Vote for best robot!
  - ▶ Robots at: <https://piazza.com/class/j7todrhr6a74af?cid=546>
  - ▶ Vote at: <https://piazza.com/class/j7todrhr6a74af?cid=582>

# Normal Transformation

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- ▶ Why transform normal vectors with inverse transpose of a transformation matrix?



- ▶ Middle image: normal scaled like geometry gives wrong result

<https://paroj.github.io/gltut/Illumination/Tut09%20Normal%20Transformation.html>

# More Realistic Illumination

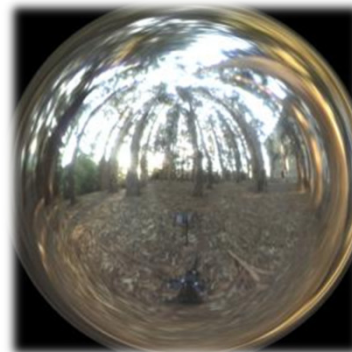
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- ▶ In the real world:
  - At each point in scene light arrives from all directions
    - ▶ Not just from a few point light sources
    - ▶ → Global Illumination is a solution, but computationally expensive
- ▶ Environment Maps
  - ▶ Store “omni-directional” illumination as images
  - ▶ Each pixel corresponds to light from a certain direction
  - ▶ Sky boxes make for great environment maps



# Capturing Environment Maps

- ▶ Environment map = surround panoramic image
- ▶ Creating 360 degrees panoramic images:
  - ▶ 360 degree camera
  - ▶ “light probe” image: take picture of mirror ball (e.g., silver Christmas ornament)



Light Probes by Paul Debevec  
<http://www.debevec.org/Probes/>

# Environment Maps as Light Sources

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## **Simplifying Assumption**

- ▶ Assume light captured by environment map is emitted from infinitely far away
- ▶ Environment map consists of directional light sources
  - ▶ Value of environment map is defined for each **direction**, independent of position in scene
- ▶ Approach uses same environment map at each point in scene  
→ Approximation!

# Applications for Environment Maps

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- ▶ Use environment map as “light source”



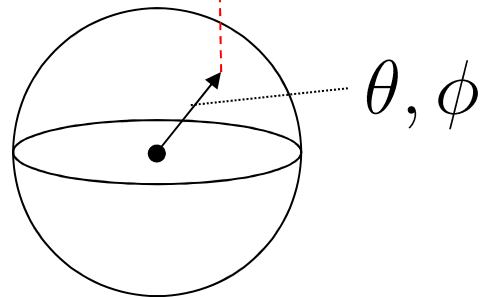
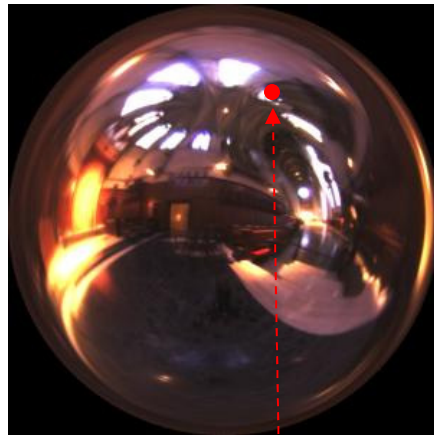
*Global illumination with  
pre-computed radiance transfer  
[Sloan et al. 2002]*



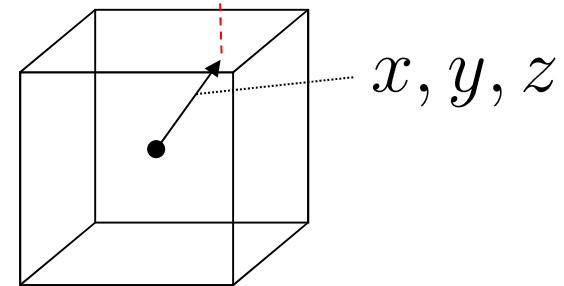
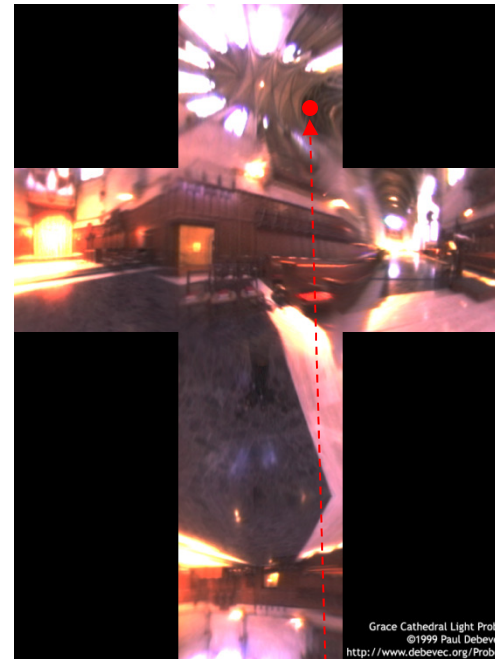
*Reflection mapping  
[Georg-Simon Ohm University of Applied Sciences]*

# Cubic Environment Maps

- Store incident light on six faces of a cube instead of on sphere



Spherical map



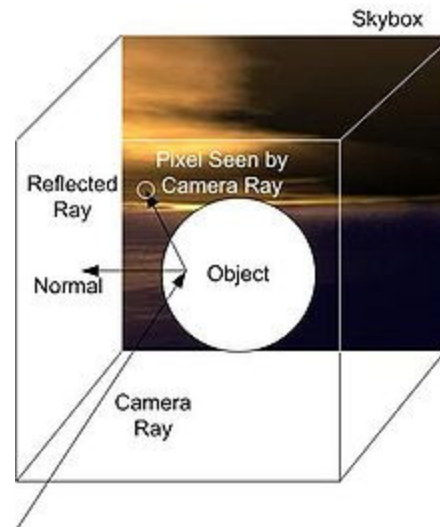
Cube map



# Cubic vs. Spherical Maps

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- ▶ **Advantages of cube maps:**
  - ▶ More even texel sample density causes less distortion, allowing for lower resolution maps
  - ▶ Easier to dynamically generate cube maps for real-time simulated reflections



# Bubble Demo

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<http://download.nvidia.com/downloads/nZone/demos/nvidia/Bubble.zip>

# Cubic Environment Maps

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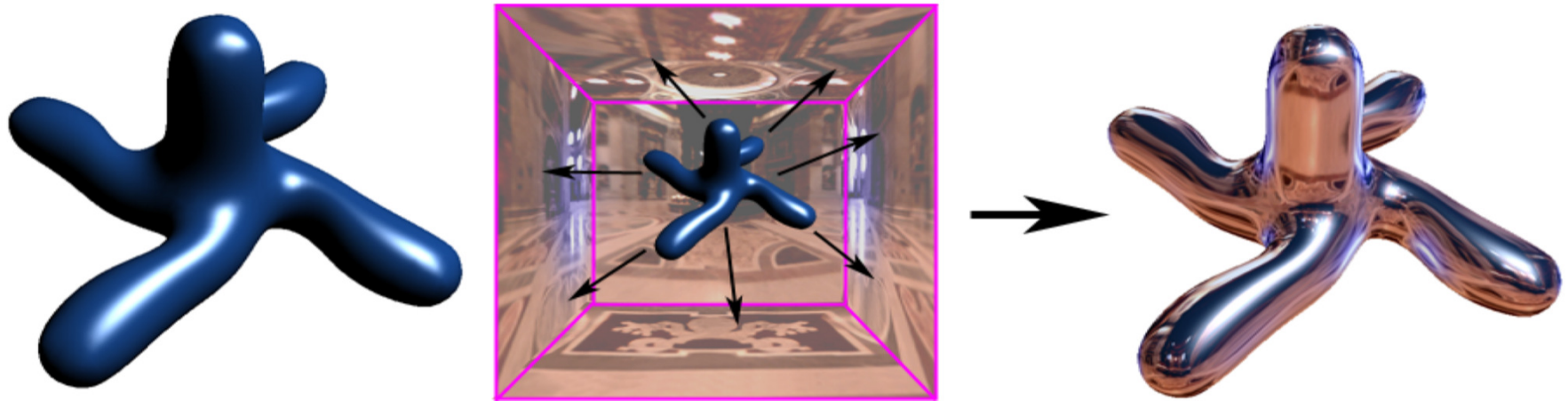
## Cube map look-up

- ▶ Given: light direction  $(x,y,z)$
- ▶ Largest coordinate component determines cube map face
- ▶ Dividing by magnitude of largest component yields coordinates within face
- ▶ In GLSL:
  - ▶ Use  $(x,y,z)$  direction as texture coordinates to `samplerCube`

# Reflection Mapping

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- ▶ Simulates mirror reflection
- ▶ Computes reflection vector at each pixel
- ▶ Use reflection vector to look up cube map
- ▶ Rendering cube map itself is optional (application dependent)



Reflection mapping

# Reflection Mapping in GLSL

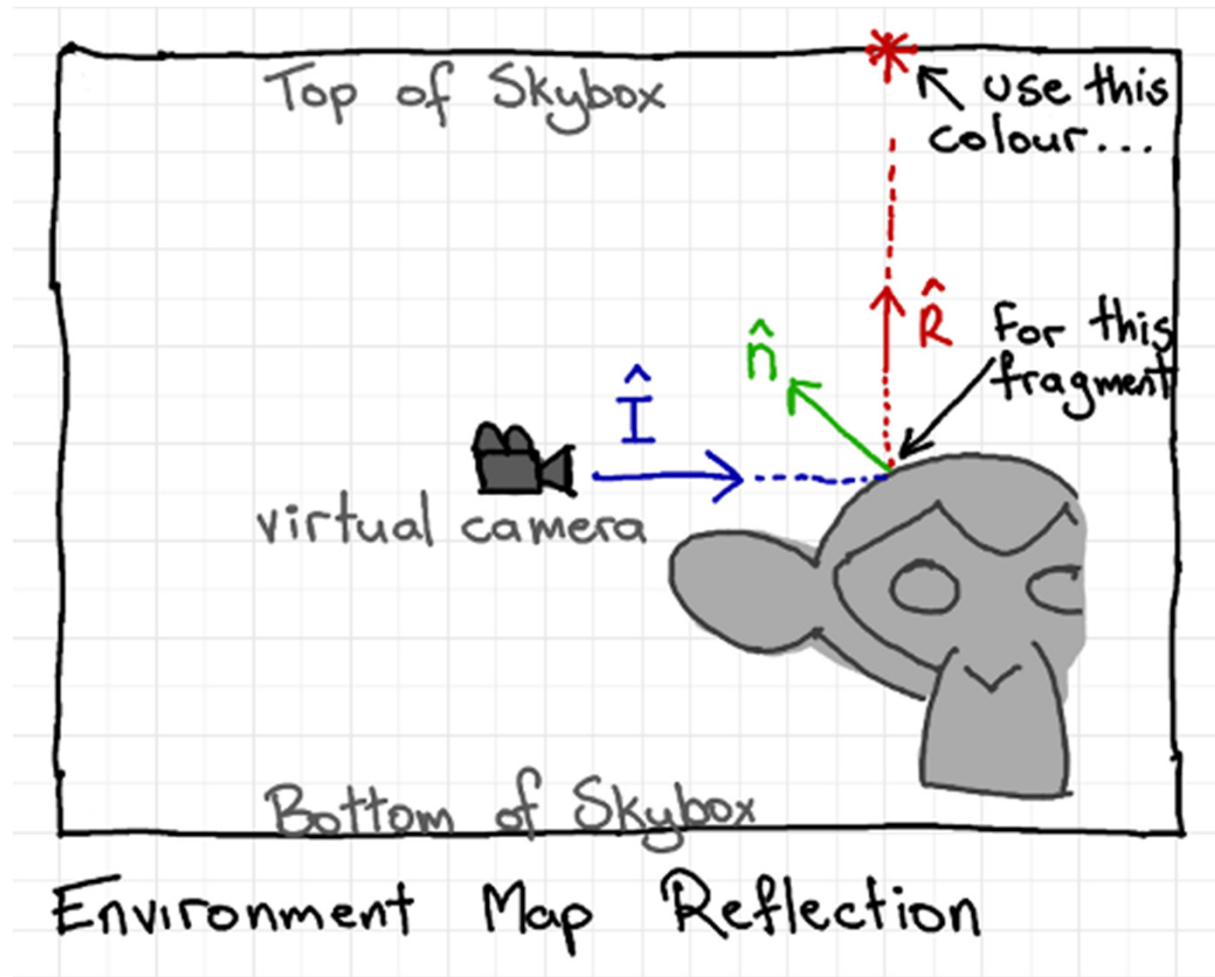
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## Application Setup

### ► Load and bind a cube environment map

```
glBindTexture(GL_TEXTURE_CUBE_MAP, ...);  
glTexImage2D(GL_TEXTURE_CUBE_MAP_POSITIVE_X, ...);  
glTexImage2D(GL_TEXTURE_CUBE_MAP_NEGATIVE_X, ...);  
glTexImage2D(GL_TEXTURE_CUBE_MAP_POSITIVE_Y, ...);  
...  
glEnable(GL_TEXTURE_CUBE_MAP);
```

# Environment Mapping: Concept



Source: <http://antongerdelan.net/opengl/cubemaps.html>

# Environment Mapping: Vertex Shader

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```
#version 400

in vec3 vp; // positions from mesh
in vec3 vn; // normals from mesh
uniform mat4 P, V, M; // proj, view, model matrices
out vec3 pos_eye;
out vec3 n_eye;

void main()
{
    pos_eye = vec3(V * M * vec4(vp, 1.0));
    n_eye = vec3(V * M * vec4(vn, 0.0));
    gl_Position = P * V * M * vec4(vp, 1.0);
}
```

# Environment Mapping: Fragment Shader

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```
#version 400

in vec3 pos_eye;
in vec3 n_eye;
uniform samplerCube cube_texture;
uniform mat4 V; // view matrix
out vec4 frag_colour;

void main()
{
    // reflect ray around normal from eye to surface
    vec3 incident_eye = normalize(pos_eye);
    vec3 normal = normalize(n_eye);

    vec3 reflected = reflect(incident_eye, normal);
    // convert from eye to world space
    reflected = vec3(inverse(V) * vec4(reflected, 0.0));

    frag_colour = texture(cube_texture, reflected);
}
```



# Environment Maps as Light Sources

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- ▶ Covered so far: shading of a specular surface
- How do you compute shading of a diffuse surface?

# Diffuse Irradiance Environment Map

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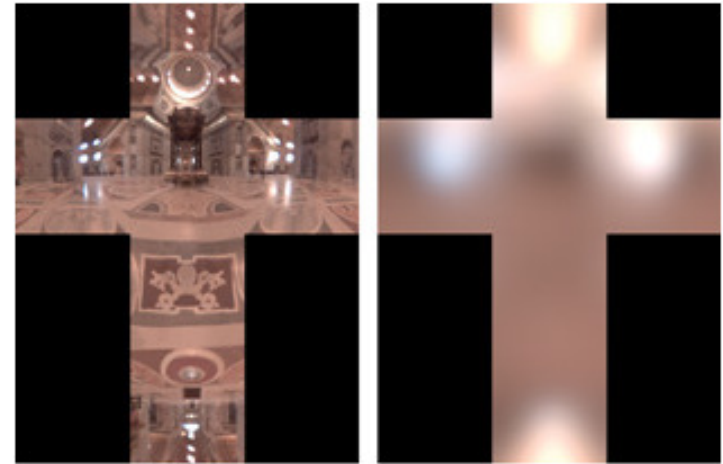
- ▶ Given a scene with  $k$  directional lights, light directions  $d_1..d_k$  and intensities  $i_1..i_k$ , illuminating a diffuse surface with normal  $n$  and color  $c$
- ▶ Pixel intensity  $B$  is computed as: 
$$B = c \sum_{j=1..k} \max(0, d_j \cdot n) i_j$$
- ▶ Cost of computing  $B$  proportional to number of texels in environment map!
- ▶ → Precomputation of diffuse reflection
- ▶ Observations:
  - ▶ All surfaces with normal direction  $n$  will return the same value for the sum
  - ▶ The sum is dependent on just the lights in the scene and the surface normal
- ▶ Precompute sum for any normal  $n$  and store result in a second environment map, indexed by surface normal
- ▶ Second environment map is called *diffuse irradiance environment map*
- ▶ Allows to illuminate objects with arbitrarily complex lighting environments with single texture lookup

# Diffuse Irradiance Environment Map

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- ▶ Two cubic environment maps:

- ▶ Reflection map
  - ▶ Diffuse map



- ▶ Diffuse shading vs. shading w/diffuse map



Image source: [http://http.developer.nvidia.com/GPUGems2/gpugems2\\_chapter10.html](http://http.developer.nvidia.com/GPUGems2/gpugems2_chapter10.html)