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# CSE 167

Discussion 01 ft. Yining  
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# Announcements

- Private posts are for **emergencies** or a question that explicitly shows a part of your code
- Office hour schedule is up on Piazza
- Project 1 is due next Friday

# Contents

- Starter code overview
- Linear algebra
  - Homogeneous coordinate
  - MVP matrices
  - Matrix multiplication
- glm functions

# Starter code overview: OBJObject

- What is an “object”?
  - A “thing” that you would like to place in your scene
- Where to create an object?
  - Hopefully, the same place where cube was created
- What functions need to be in OBJObject?
  - parse(): for parsing .obj files
    - Make sure you are NOT parsing vertex normals as vertices!!!
    - The number of vertices specified in .obj file should be the same as the number of parsed vertex lines
  - some\_function(): for spinning the object
  - Matrix operation helper functions: for translation, scaling, orbiting, and resetting
    - Pay attention to the matrix multiplication order!!!

```
#####  
#  
# OBJ File Generated by Meshlab  
#  
#####  
# Object bunny_n.obj  
#  
# Vertices: 34835  
# Faces: 6966  
#  
#####  
vn -1.345425 -4.896516 -1.808985  
v 0.296502 -0.907931 0.450151 0.752941 0.752941 0.752941  
vn -2.353551 -5.669106 -0.381383  
v 0.315114 -0.913622 0.435867 0.752941 0.752941 0.752941  
vn -3.331857 -4.821201 -1.723500  
v 0.324517 -0.920404 0.443869 0.752941 0.752941 0.752941
```

# Starter code overview: Window

- `Window::initialize_objects()`
  - DON'T parse an object every time you switch, parse them all at once in the beginning
  - bear.obj alone has 866,394 vertices, if you parse it every time you switch back to bear, it's going to take a lot of time...
- `Window::idle_callback()`
  - You need to spin bunny/dragon/bear constantly; that means you need to do something here
- `Window::display_callback()`
  - Here, you will call the `draw()` function
- `Window::key_callback()`
  - You specify what to do when a certain key is pressed

# Linear algebra: homogenous coordinate

- $(xz, yz, z)$  is called a set of homogenous coordinates of  $(x, y)$ 
  - Note that since **z is nonzero**,  $(xz, yz, z)$  can also be written as  $(x, y, 1)$
- What does this mean geometrically?
  - Chalkboard time
- Why do we need this?
  - Given  $(x, y, z)$  we can extend this to a homogenous coordinate  $(x, y, z, w)$  with  $w = 1$
  - This means a 3D point can be represented as a 4D vector
  - Then we can multiply  $4 \times 4$  matrices and  $4 \times 1$  vectors
  - So what?

# Linear algebra: homogenous coordinate

Let  $R_y$  be a rotation matrix with respect to the y-axis and  $\theta = 90^\circ$ :

$$R_y = \begin{bmatrix} \cos\theta & 0 & \sin\theta \\ 0 & 1 & 0 \\ -\sin\theta & 0 & \cos\theta \end{bmatrix} = \begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ -1 & 0 & 0 \end{bmatrix}$$

And let  $T$  be a translation vector:

$$T = \begin{bmatrix} 0 \\ 2 \\ 3 \end{bmatrix}$$

To rotate a point  $A(-1, 0, 0)$  by 90 degrees and then translate by  $T$ :

$$A' = R_y \cdot A + T$$

In other words,

$$A' = \begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ -1 & 0 & 0 \end{bmatrix} \begin{bmatrix} -1 \\ 0 \\ 0 \end{bmatrix} + \begin{bmatrix} 0 \\ 2 \\ 3 \end{bmatrix} = \begin{bmatrix} 0 \\ 2 \\ 4 \end{bmatrix}$$

So this is a combination of matrix multiplication AND matrix addition.

# Linear algebra: homogenous coordinate

But what if you started off with  $4 \times 4$  matrices and  $4 \times 1$  vector in the first place?

$$R_y = \begin{bmatrix} \cos\theta & 0 & \sin\theta & 0 \\ 0 & 1 & 0 & 0 \\ -\sin\theta & 0 & \cos\theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \text{ and } T = \begin{bmatrix} 1 & 0 & 0 & t_x \\ 0 & 1 & 0 & t_y \\ 0 & 0 & 1 & t_z \\ 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 2 \\ 0 & 0 & 1 & 3 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

And let  $A(-1, 0, 0, 1)$ . Then,

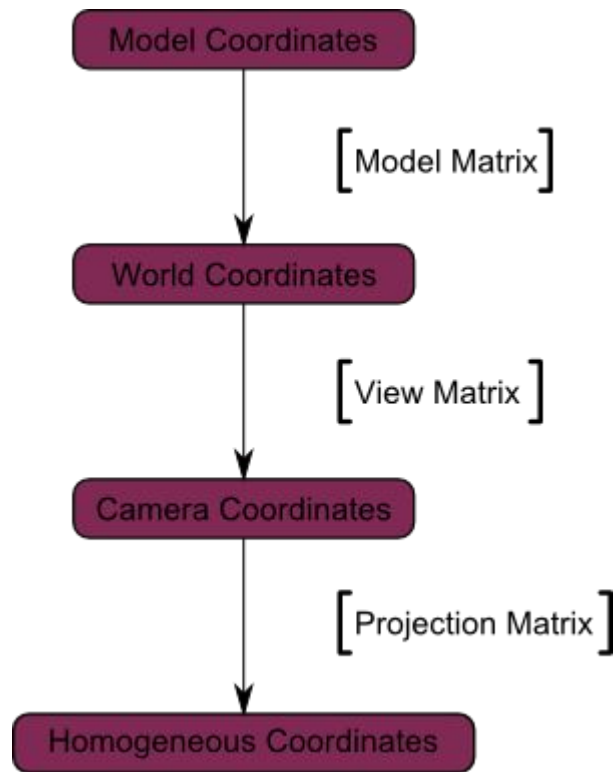
$$A' = T \cdot R_y \cdot A$$

In other words, using homogenous coordinate and  $4 \times 4$  transformation matrices, we can transform a point by just a series of matrix multiplications.



# Linear algebra: MVP matrices

- M: place the object
- V: place the camera
- P: set up the camera
- Chalkboard time



# Linear algebra: matrix multiplication

- In what order do we multiply?
  - Let's say I have a transformation matrix  $M$  that was the result of the previous example
  - If I want to rotate an object with respect to **the world's y-axis**, which one is right?
    - $M = R * M$ ?
    - $M = M * R$ ?
  - If I want to rotate an object with respect to **its own y-axis** again, which one is right?
    - $M = R * M$ ?
    - $M = M * R$ ?
- If you understood this part, you now know what  $M$  is actually the "toWorld" matrix in the starter code

# glm functions

- `glm::translate()`
- `glm::rotate()`
- `glm::scale()`
  
- `glm::lookAt()`
  
- `glm::perspective()`