CSE 167: Introduction to Computer Graphics Lecture #6: Color

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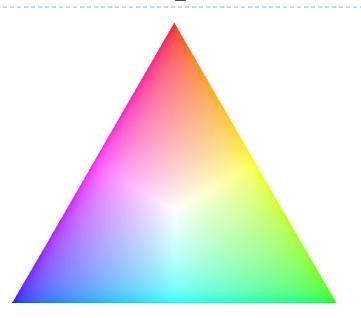
Announcements

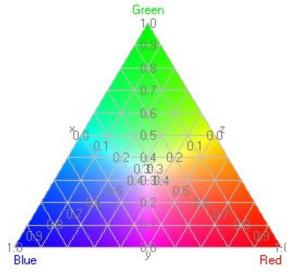
- ▶ Homework project #3 due this Friday, October 19
 - ▶ To be presented starting 1:30pm in lab 260
 - ▶ Late submissions for project #2 accepted
- Please check grades in Ted
- Any problems with Ted?
 - Discussion groups
 - Grades

Lecture Overview

Review: Barycentric Coordinates

Color Interpolation



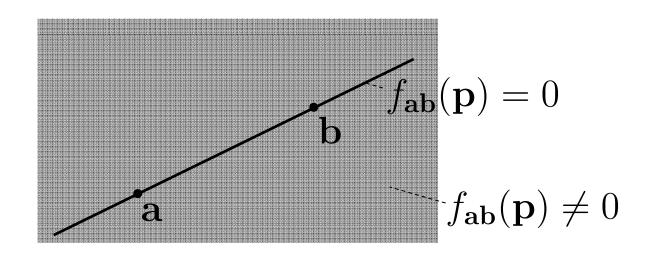


Source: efg's computer lab

- What if a triangle's vertex colors are different?
- Need to interpolate across triangle
 - How to calculate interpolation weights?

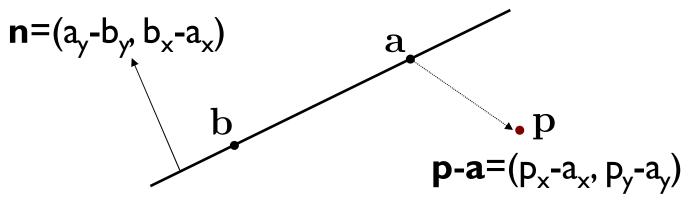
Implicit 2D Lines

- Given two 2D points a, b
- ▶ Define function $f_{ab}(\mathbf{p})$ such that $f_{ab}(\mathbf{p}) = 0$ if \mathbf{p} lies on the line defined by \mathbf{a} , \mathbf{b}



Implicit 2D Lines

Point p lies on the line, if p-a is perpendicular to the normal n of the line

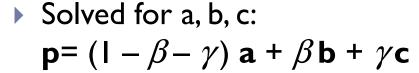


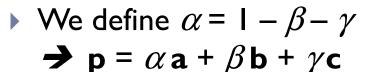
▶ Use dot product to determine on which side of the line p lies. If f(p)>0, p is on same side as normal, if f(p)<0 p is on opposite side. If dot product is 0, p lies on the line.</p>

$$f_{ab}(\mathbf{p}) = (a_y - b_y, b_x - a_x) \cdot (p_x - a_x, p_y - a_y)$$

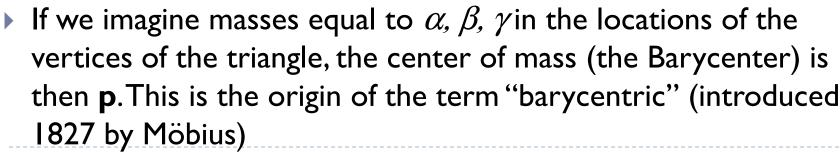
Barycentric Coordinates

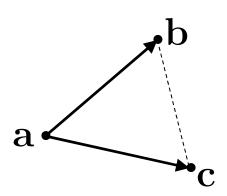
- Coordinates for 2D plane defined by triangle vertices a, b, c
- Any point **p** in the plane defined by **a**, **b**, **c** is $\mathbf{p} = \mathbf{a} + \beta(\mathbf{b} \mathbf{a}) + \gamma(\mathbf{c} \mathbf{a})$





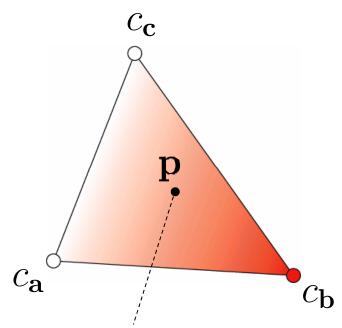






Barycentric Interpolation

Interpolate values across triangles, e.g., colors



Done by linear interpolation on triangle:

$$c(\mathbf{p}) = \alpha(\mathbf{p})c_{\mathbf{a}} + \beta(\mathbf{p})c_{\mathbf{b}} + \gamma(\mathbf{p})c_{\mathbf{c}}$$

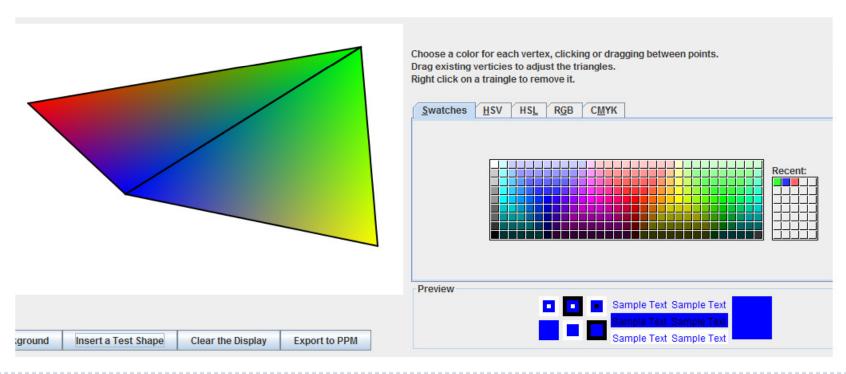
Works well at common edges of neighboring triangles

Barycentric Coordinates

Demo Applet:

http://www.ccs.neu.edu/home/suhail/BaryTriangles/applet.htm

Barycentric Coordinates Applet



Lecture Overview

Color

- Physical background
- Color perception
- Color spaces

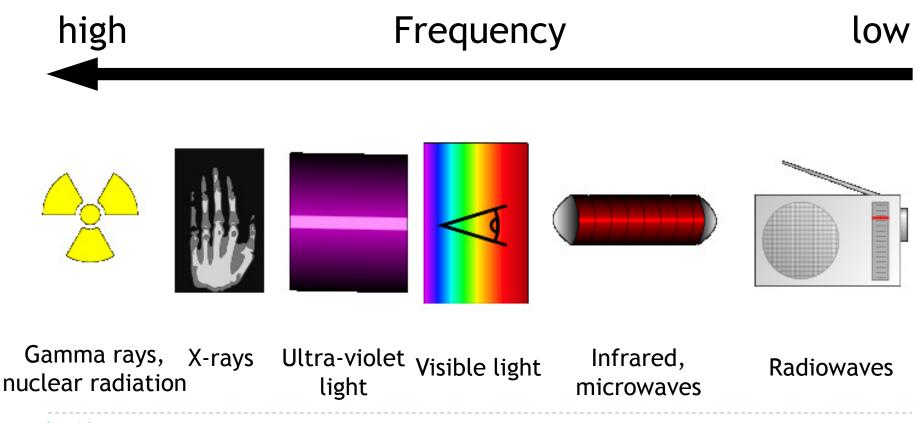
Light

Physical models

- Electromagnetic waves [Maxwell 1862]
- Photons (tiny particles) [Planck 1900]
- Wave-particle duality [Einstein, early 1900] "It depends on the experiment you are doing whether light behaves as particles or waves"
- Simplified models in computer graphics

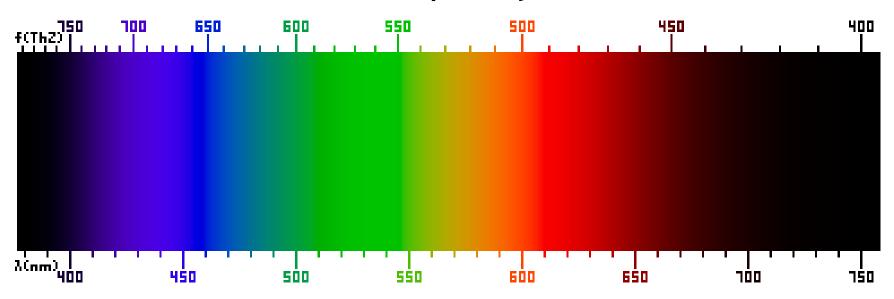
Electromagnetic Waves

Large range of frequencies



Visible Light

Frequency



Wavelength: 1nm=10^-9 meters speed of light = wavelength * frequency

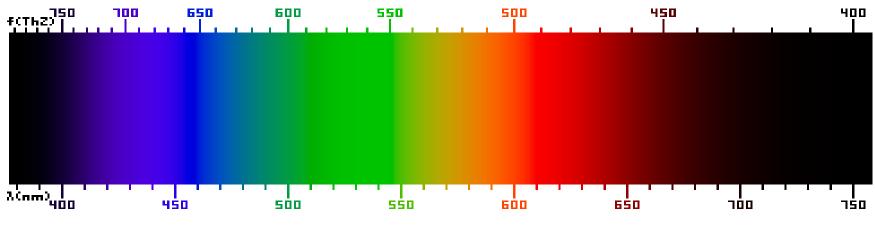
Example 91.1MHz:

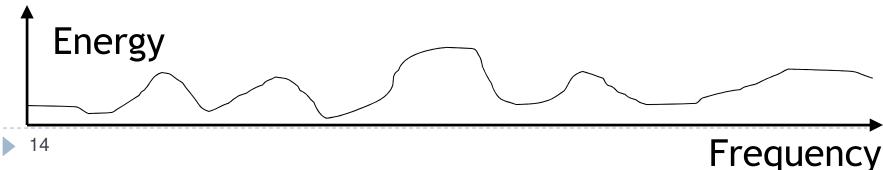
$$\frac{300*10^6 \frac{m}{s}}{91.1*10^6 \frac{1}{s}} = 3.29m$$

Light Transport

Simplified model in computer graphics

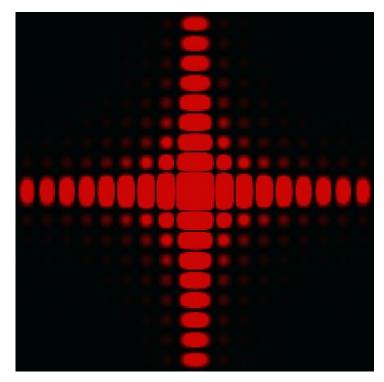
- ▶ Light is transported along straight rays
- ▶ Rays carry a spectrum of electromagnetic energy





Limitations

- OpenGL ignores wave nature of light
 - → no diffraction effects



Diffraction pattern of a small square aperture



Surface of a CD shows diffraction grating

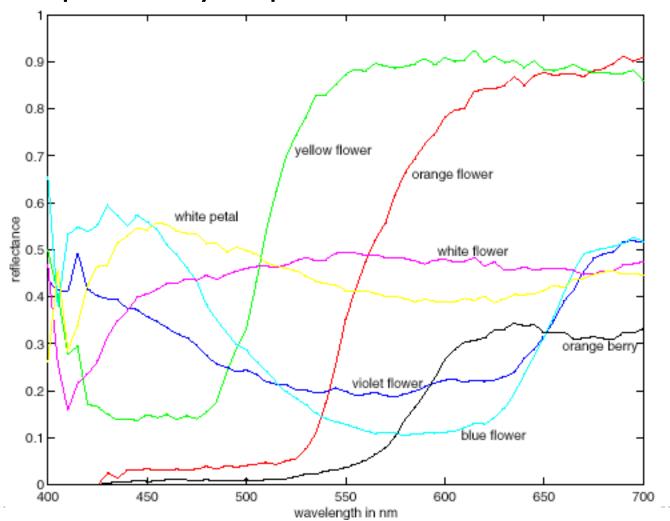
Lecture Overview

Color

- Physical background
- Color perception
- Color spaces

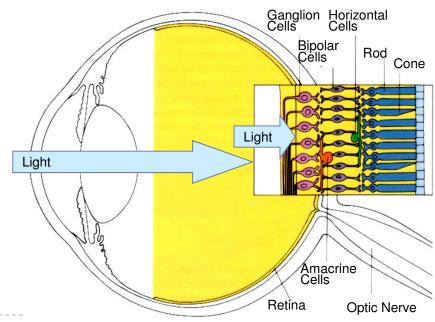
Light and Color

Different spectra may be perceived as the same color

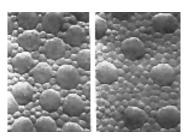


Color Perception

- Photoreceptor cells
- Light sensitive
- ▶ Two types, rods and cones







Distribution of Cones and Rods

Rods

- ▶ More than 1,000 times more sensitive than cones
- Low light vision
- Brightness perception only, no color
- Predominate in peripheral vision

Cones

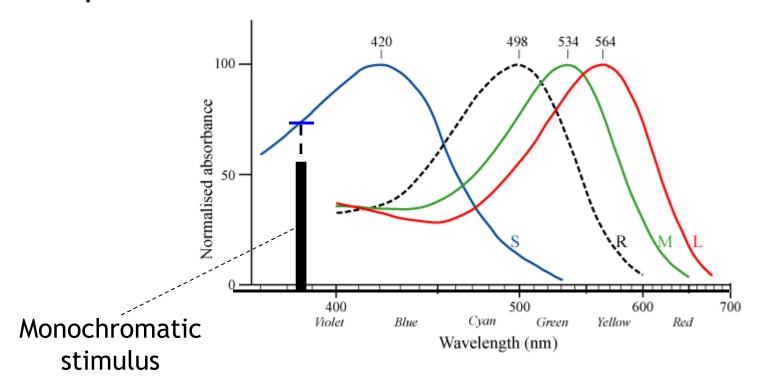
- Responsible for high-resolution vision
- ▶ 3 types of cones for different wavelengths (LMS):
 - L: long, red
 - M: medium, green
 - S: short, blue

The Austrian naturalist Karl von Frisch has demonstrated that honeybees, although blind to red light, distinguish at least four different color regions, namely:

- yellow (including orange and yellow green)
- blue green
- blue (including purple and violet)
- ultraviolet

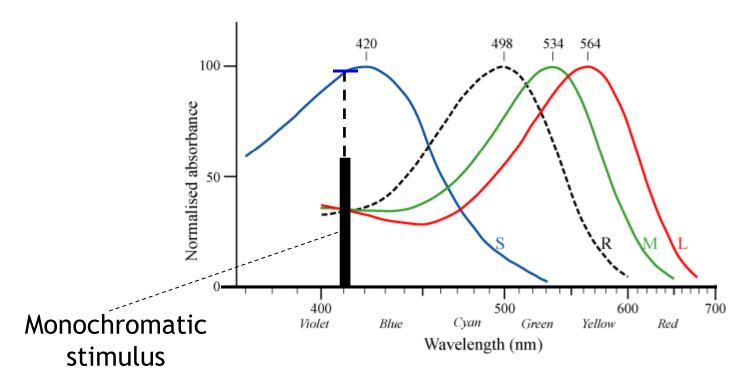
(Source: Encyclopedia Britannica)

 \blacktriangleright Response curves $s(\lambda), m(\lambda), l(\lambda)$ to monochromatic spectral stimuli



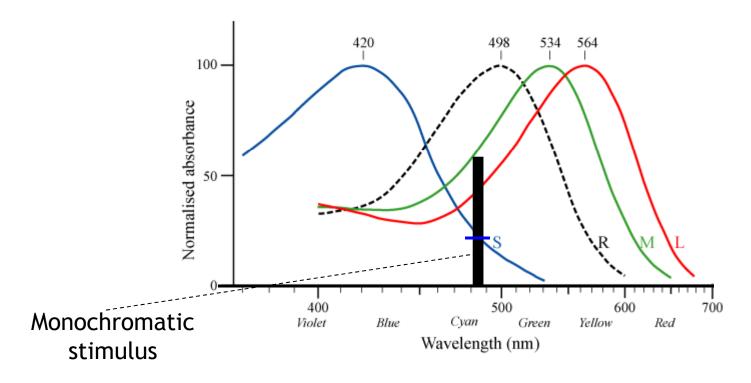
Experimentally determined in the 1980s

Response curves $s(\lambda), m(\lambda), l(\lambda)$ to monochromatic spectral stimuli



Experimentally determined in the 1980s

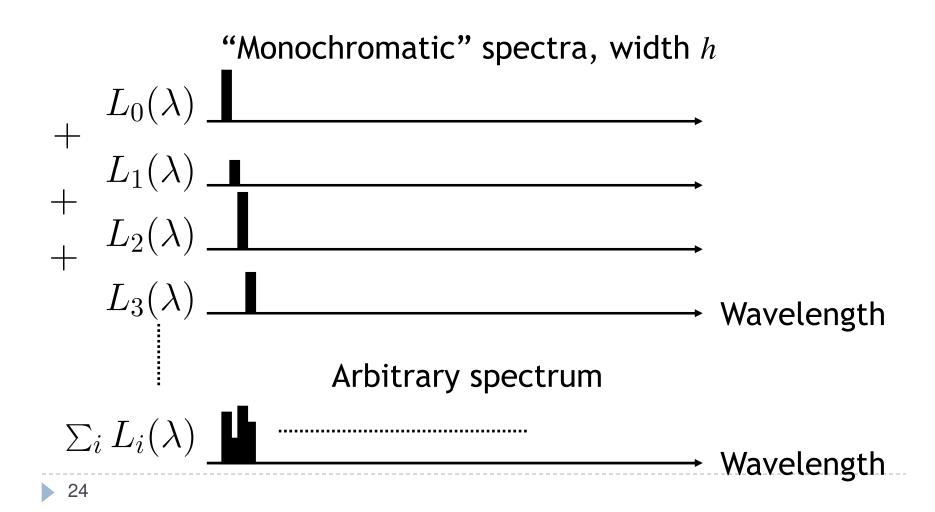
 \blacktriangleright Response curves $\;s(\lambda), m(\lambda), l(\lambda)$ to monochromatic spectral stimuli



Experimentally determined in the 1980s

Response to Arbitrary Spectrum

Arbitrary spectrum as sum of "mono-chromatic" spectra



Response to Arbitrary Spectrum

Assume linearity (superposition principle)

- Response to sum of spectra is equal to sum of responses to each spectrum
- S-cone response_s = $\sum_{i} s(\lambda) h L_i(\lambda)$

Input: light intensity $L(\lambda)$ impulse width h Response to monochromatic impulse $s(\lambda)$

In the limit $h \rightarrow 0$

$$response_s = \int s(\lambda)L(\lambda)d\lambda$$

Response to Arbitrary Spectrum

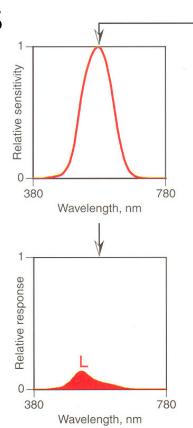
Stimulus

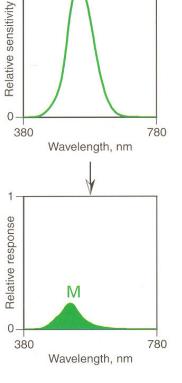
To wavelength, nm

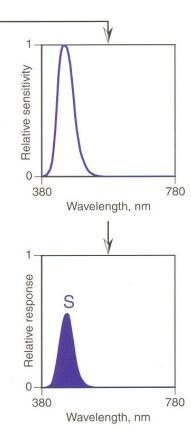
Response curves

Multiply

Integrate

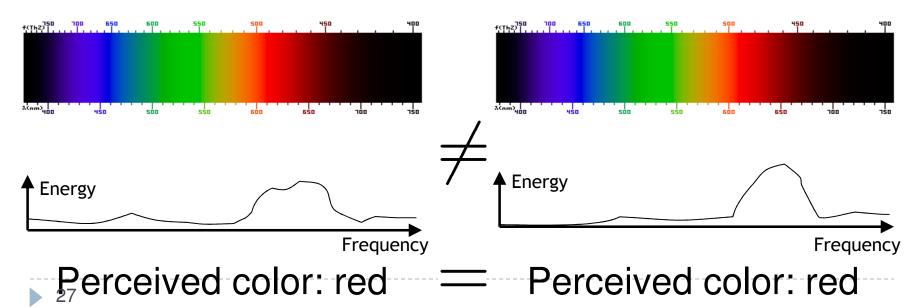






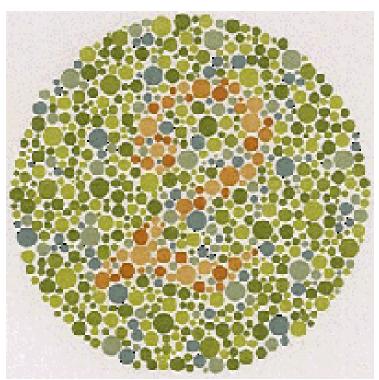
Metamers

- Different spectra, same response
- Cannot distinguish spectra
 - Arbitrary spectrum is *infinitely dimensional* (has infinite number of degrees of freedom)
 - Response has three dimensions
 - Information is lost



Color Blindness

- One type of cone missing, damaged
- Different types of color blindness, depending on type of cone
- Can distinguish even fewer colors
- But we are all a little color blind...



Lecture Overview

Color

- Physical background
- Color perception
- Color spaces

Color Reproduction

- ▶ How can we reproduce, represent color?
 - One option: store full spectrum
- Representation should be as compact as possible
- Any pair of colors that can be distinguished by humans should have two different representations

Color Spaces

- Set of parameters describing a color sensation
- "Coordinate system" for colors
- Three types of cones, expect three parameters to be sufficient
- Why not use L,M,S cone responses?

Color Spaces

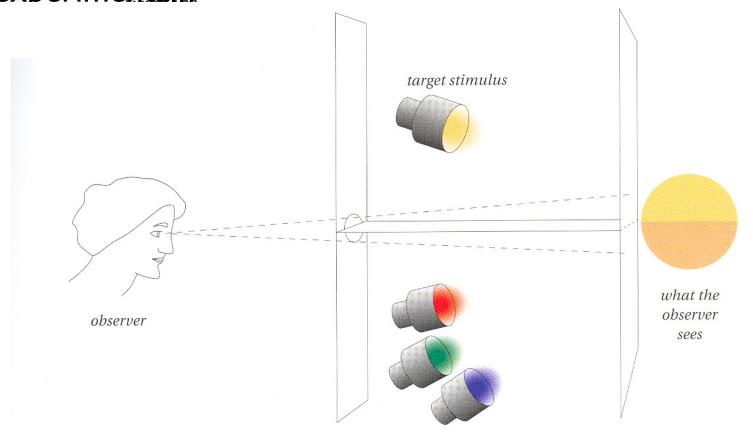
- Set of parameters describing a color sensation
- "Coordinate system" for colors
- Three types of cones, expect three parameters to be sufficient
- Why not use L,M,S cone responses?
 - Not known until 1980s!

Trichromatic Theory

- Claims any color can be represented as a weighted sum of three primary colors
- Propose red, green, blue as primaries
- Developed in 18th, 19th century, before discovery of photoreceptor cells (Thomas Young, Hermann von Helmholtz)

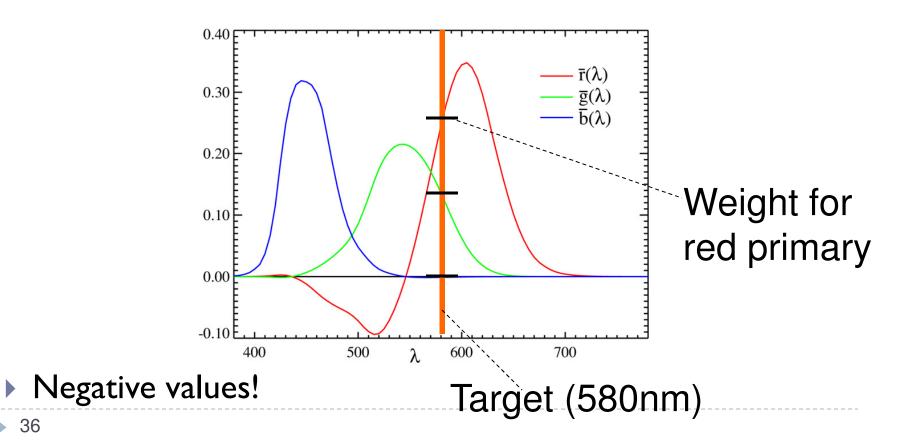
- Given arbitrary color, want to know the weights for the three primaries
- Tristimulus value
- Experimental solution
 - CIE (Commission Internationale de l'Eclairage, International Commission on Illumination), circa 1920

 Determine tristimulus values for spectral colors experimentally



The observer adjusts the intensities of the red, green, and blue lamps until they match the target stimulus on the split screen.

- Spectral primary colors were chosen
 - ▶ Blue (435.8nm), green (546.1nm), red (700nm)
- Matching curves for monochromatic target



Negative values

- Some spectral colors could not be matched by primaries in the experiment
- "Trick"
 - One primary could be added to the source (stimulus)
 - Match with the other two
 - Weight of primary added to the source is considered negative

Photoreceptor response vs. matching curve

Not the same!

Tristimulus Values

- Matching values for a sum of spectra with small spikes are the same as sum of matching values for the spikes
- ▶ Monochromatic matching curves $\bar{r}(\lambda), \bar{g}(\lambda), b(\lambda)$
- In the limit (spikes are infinitely narrow)

$$R = \int \bar{r}(\lambda)L(\lambda)d\lambda$$
$$G = \int \bar{g}(\lambda)L(\lambda)d\lambda$$
$$B = \int \bar{b}(\lambda)L(\lambda)d\lambda$$

CIE Color Spaces

- Matching curves $\bar{r}(\lambda),\bar{g}(\lambda),\bar{b}(\lambda)$ define CIE RGB color space
 - CIE RGB values are color "coordinates"
- CIE was not satisfied with range of RGB values for visible colors
- Defined CIE XYZ color space
 - Most commonly used color space today

CIE XYZ Color Space

Determined coefficients such that

- Y corresponds to an experimentally determined brightness
- No negative values in matching curves
- White is XYZ=(1/3,1/3,1/3)

Linear transformation of CIE RGB:

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \frac{1}{b_{21}} \begin{bmatrix} b_{11} & b_{12} & b_{13} \\ b_{21} & b_{22} & b_{23} \\ b_{31} & b_{32} & b_{33} \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix} = \frac{1}{0.17697} \begin{bmatrix} 0.49 & 0.31 & 0.20 \\ 0.17697 & 0.81240 & 0.01063 \\ 0.00 & 0.01 & 0.99 \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

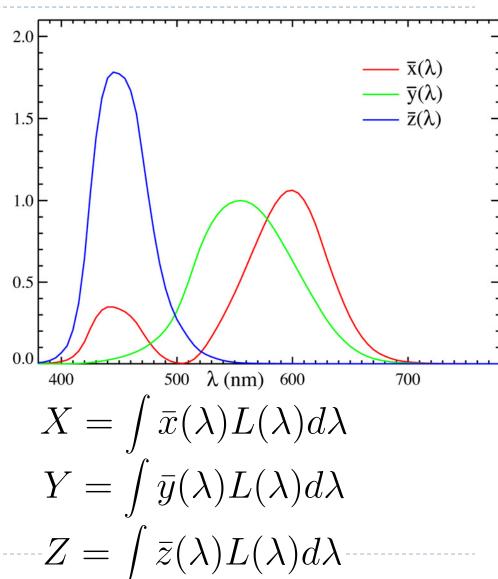
CIE XYZ Color Space

Matching curves

No corresponding physical primaries

Tristimulus values

Always positive!



Summary

- ▶ CIE color spaces are defined by matching curves
 - At each wavelength, matching curves give weights of primaries needed to produce color perception of that wavelength
 - CIE RGB matching curves determined using trisimulus experiment
- Each distinct color perception has unique coordinates
 - CIE RGB values may be negative
 - CIE XYZ values are always positive